A Moodle plug-in for Comparative Judgement

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https://github.com/ianjones/moodleCJ

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Loughborough University

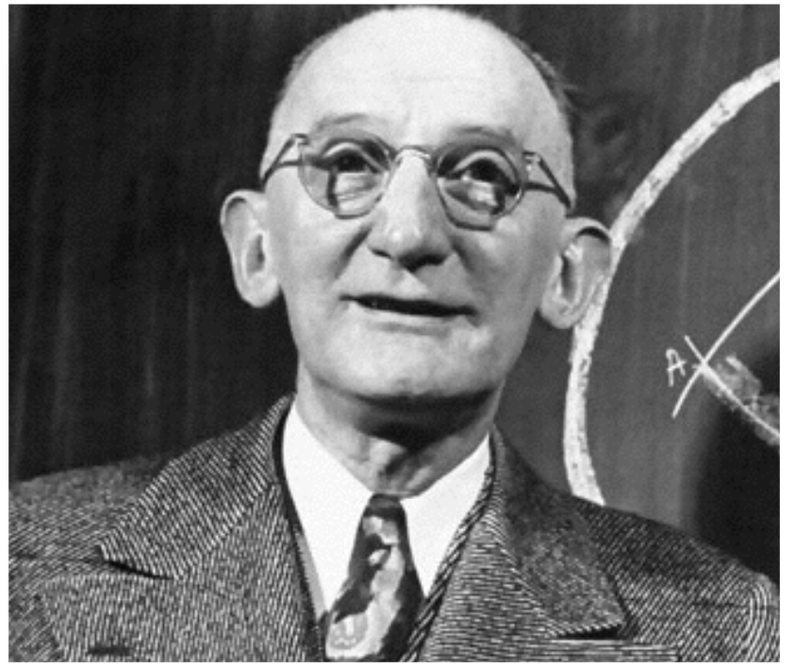
Mathematics Education Centre

High order, but hard to assess, learning constructs

- Conceptual understanding
- Proof comprehension
- Problem solving skills
- Mathematical beauty

Law of Comparative Judgement

People are inconsistent when making *absolute* judgements, and consistent when making *relative* judgements



L.L. Thurstone
(1887 - 1955)

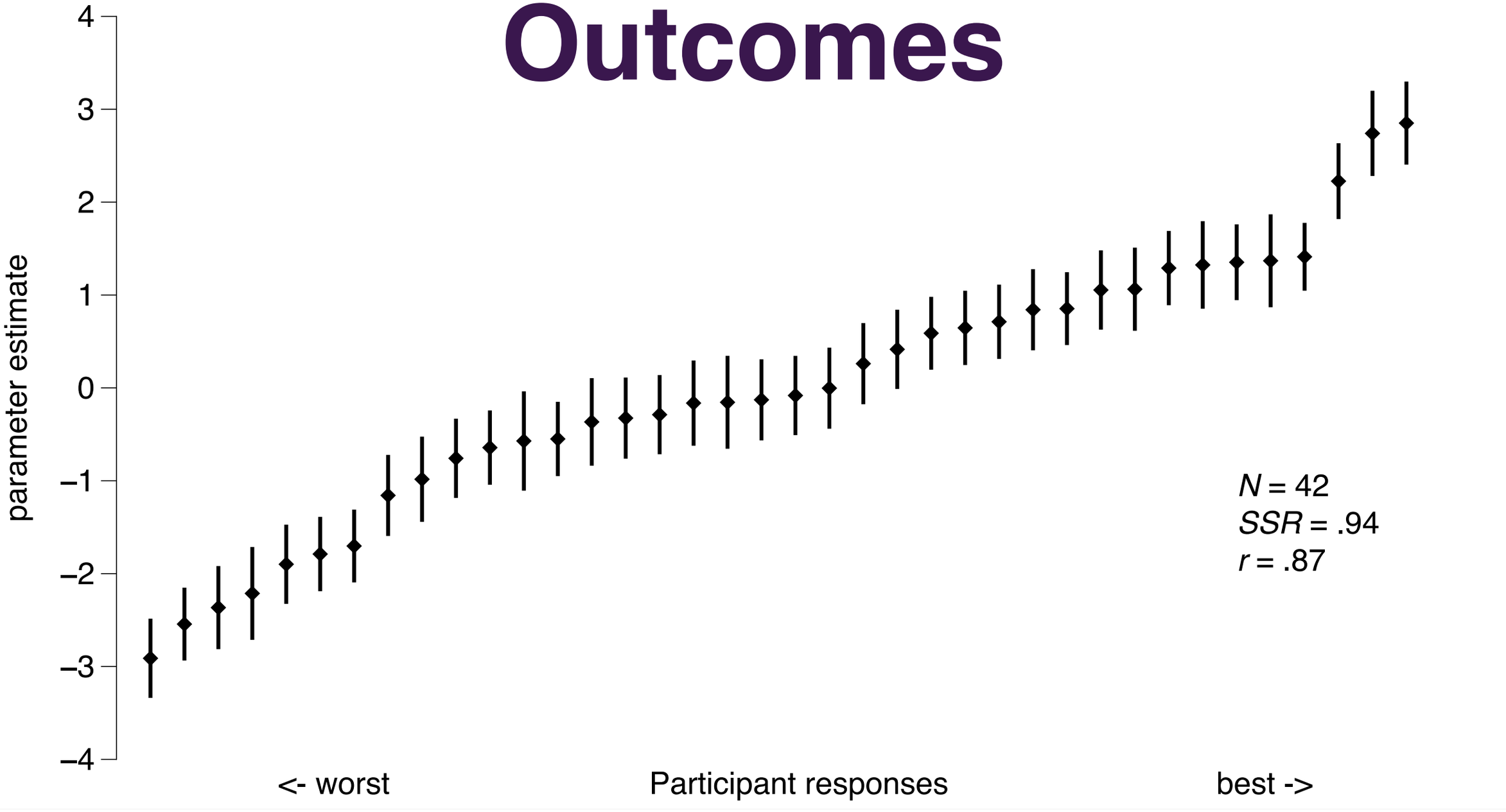
To assess high-order learning, we need

- Extended responses to open-ended prompt
- No rubrics, no coding scheme
- One high-order construct
- Judges (lecturers, peers)
- Direct pairwise comparisons of responses, via a comparative judgement engine
    - Moodle Plug-in

Typical outcomes

- Pairwise decisions
  (> 10 × number of submissions)
- Fitted to the Bradley-Terry model
- Unique score for each participant
- Reliability measures

Outcomes



- *SSR* is Scale Separation Reliability (analogous to Cronbach's alpha)
- *r* is inter-rater reliability (split-halves technique, 20 iterations)

Bisson et al. (2016)

Use case

Foundation Mathematics
at
Loughborough University

Use case

Formative peer assessment 1

Formative peer assessment 2

Formative peer assessment 3

Summative peer assessment

Open-ended task

What is an equation? Give examples of how equations can be useful.

Submit and peer assess

Choose Left

File submissions

Equations

An equation is a mathematical expression that often contains some algebra. An algebraic expression contains an unknown variable such as X or Y that you need to solve to find the value. Foe example, in the expression X + 7 = 14 you solve for X. To solve this type of expression you need to balance it by doing the same thing to one side as you do to the other. In the above example you subtract 7 from the left and right side. This leaves x = 7.

These equations can become much more complex. For example, you may see an equation like 7x + 2y – 1 = 8. To solve this, we would still need to perform the same action on both sides. The final answer for this equation is x = 1 and y=1. This type of equation asks you to solve for 2 unknown variables.

You may also be asked to solve simultaneous equations. This is when two or more different equations contain the same variables that have the same unknown variable. For example, x - y = 10 and 2x – y = 18.

This can be solved through elimination or substitution. Below is an example of elimination.

x - y –(2x-y)= 10 – 18.

x - 2x = -8

x = 8

We then put the found value into the equation.

8-y=10

8 - -2 = 10

Y=-2

Equations can be useful as it can be used to solve some where not every value is known. Equations are also useful in the real world. Equations are applied frequently in scientific formula and even in other fields such as economics and finance.

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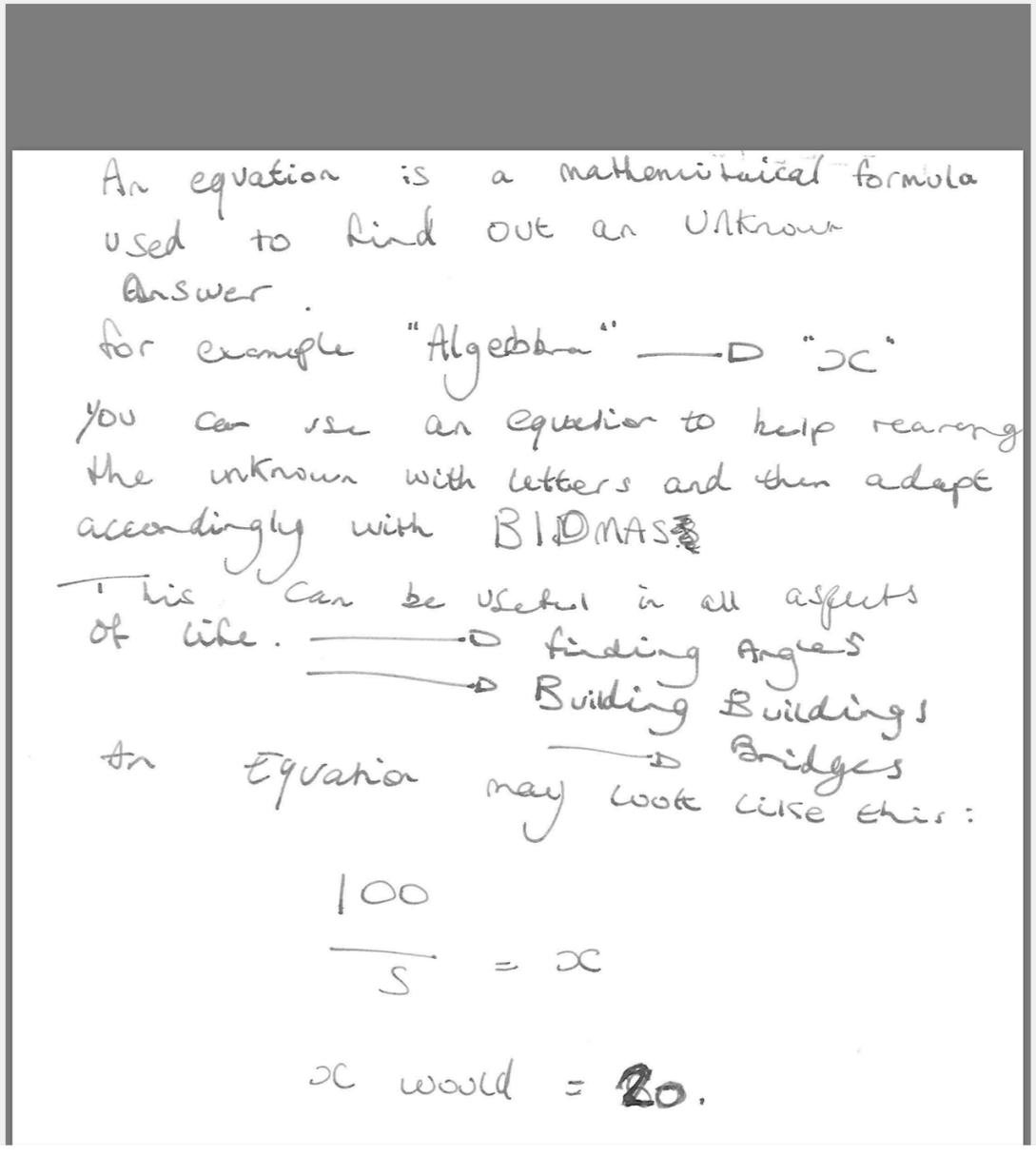
File submissions



Discussion in groups

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File submissions

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x- [illegible] 18

[illegible] value into the equation.

8-y=10

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Y=-2

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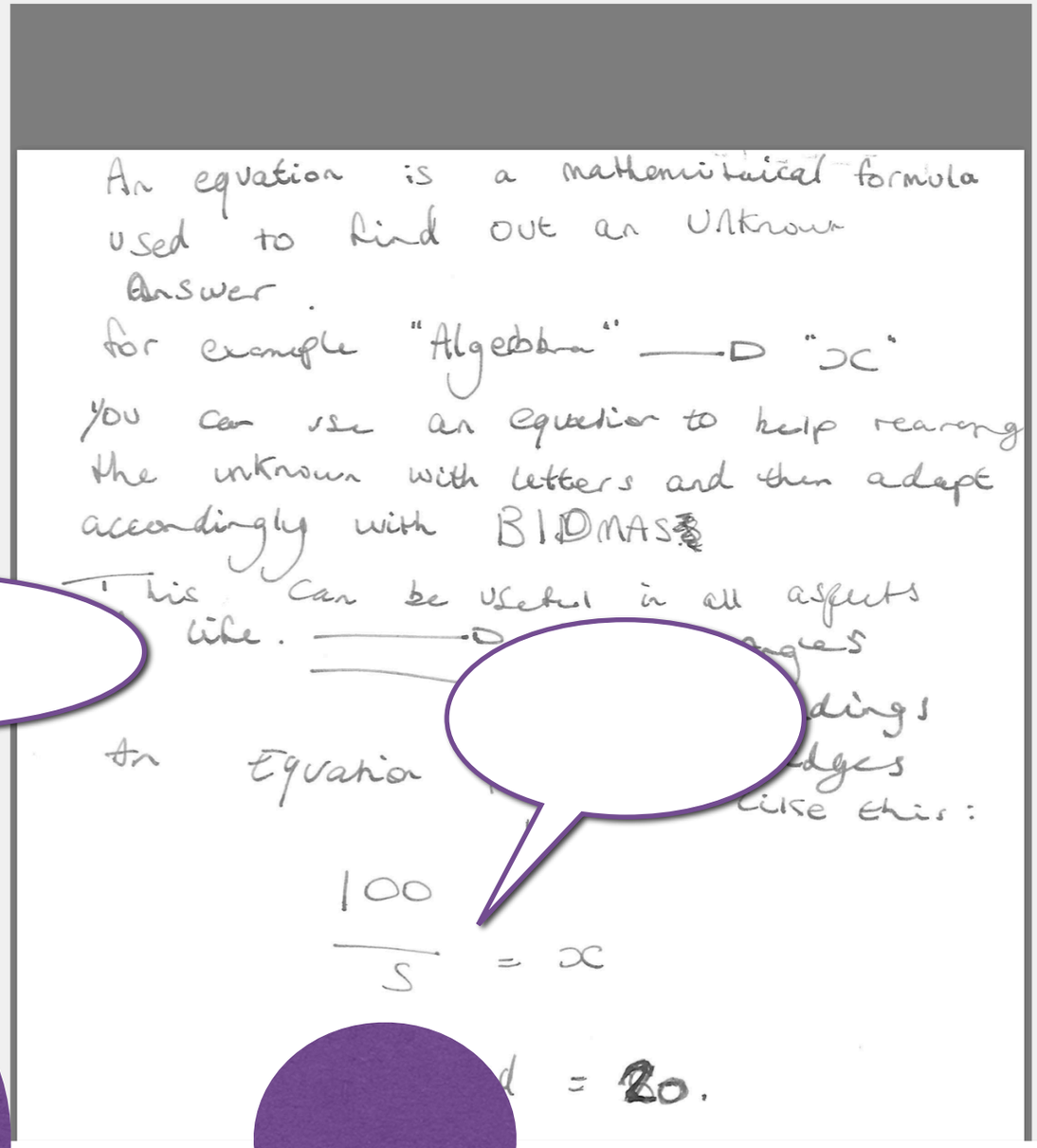
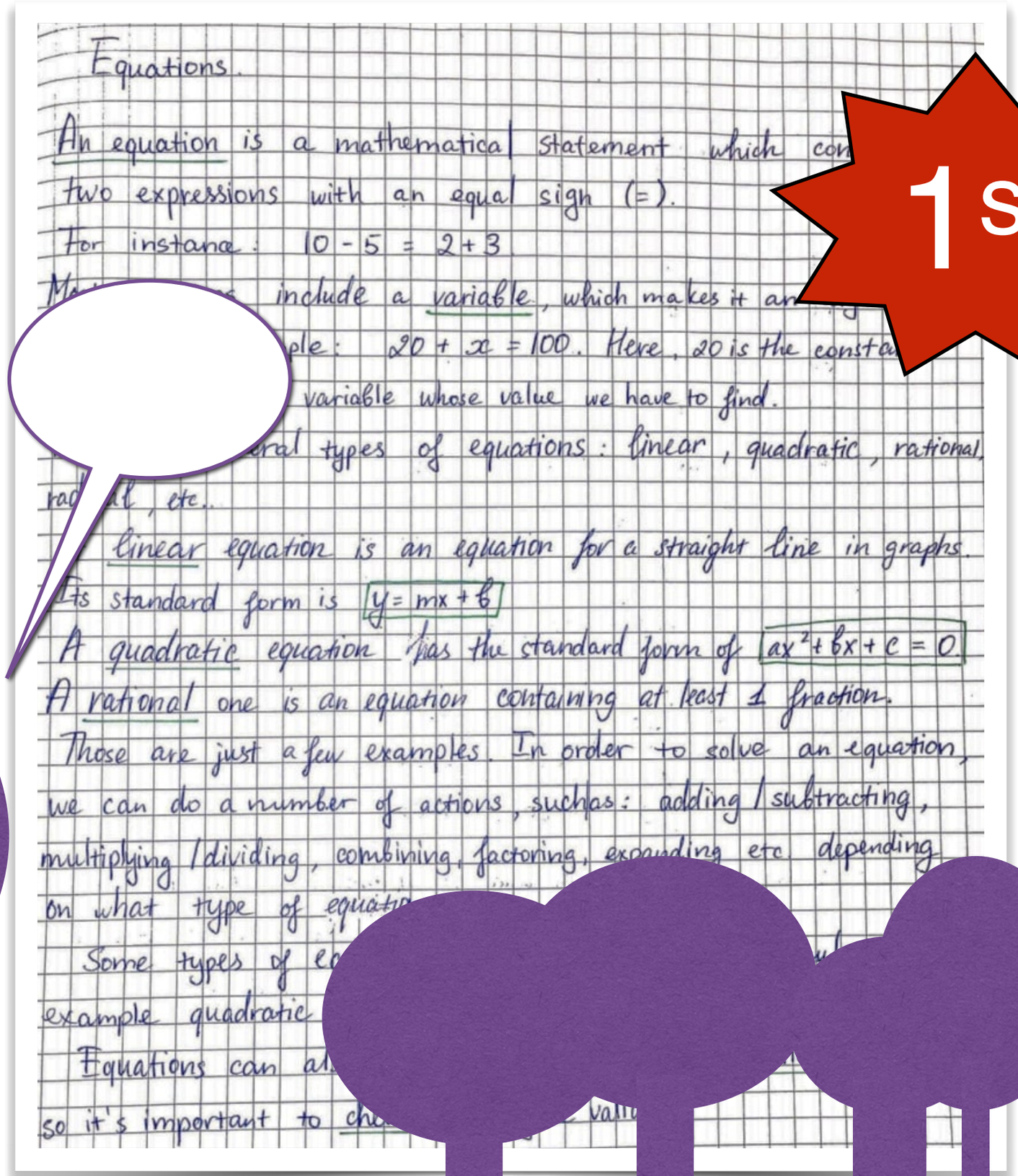
File submissions



Facilitated class discussion

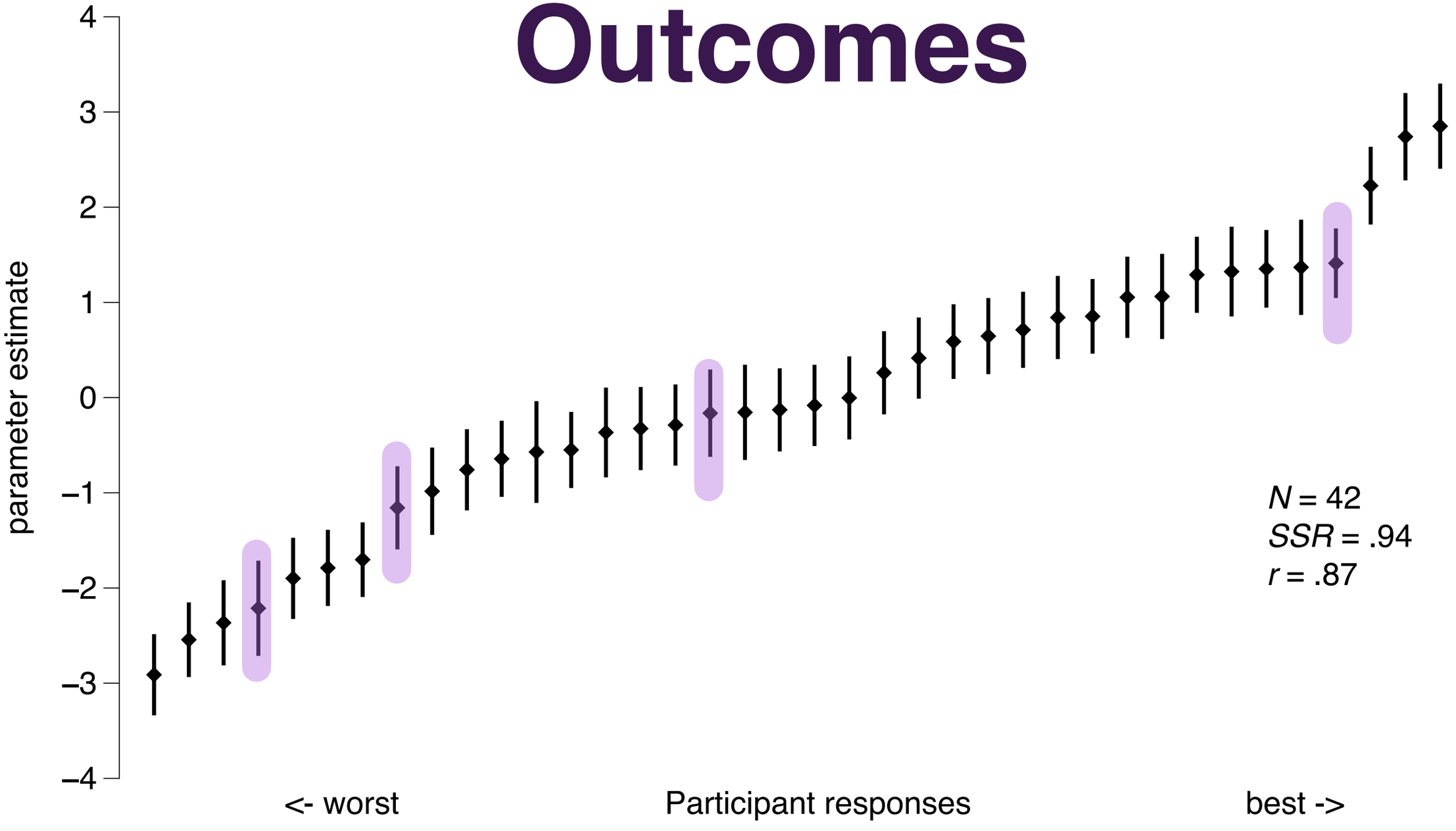


Questions and issues

Isn’t it norm-referenced?

- No, there are various methods for benchmarking comparative judgement outcomes
  (e.g. Jones & Alcock 2014; Hunter & Jones 2018)
- In fact benchmarking and standard setting is a particular strength
  (e.g. Jones et al. 2016; Heldsigner & Humphry 2013)
- You can compare unlike objects
  (e.g. Jones et al. 2016; Hunter & Jones 2018)

Outcomes



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Isn’t it opaque?

- Validity resides in the collective judgement of experts
- Varied approaches to validity reported
  - Convergent and divergent
    (e.g. Jones & Inglis 2015*;* Jones et al. 2013)
  - Content analysis
    (e.g. Hunter & Jones 2018)
  - Interviews and surveys of judges
    (e.g. Jones & Alcock 2014*;* van Daal et al. 2019)
  - Expert vs. novice vs. non-expert judges
    (e.g. Jones & Alcock 2014*;* Jones & Sirl 2017)

What about feedback?

- Students don’t get red ink on their work
- The plug-in allows judges to make comments
- We can see a rich and high-quality form of feedback when students
  - compare their peers’ work
  - discuss their peers' work in small groups
  - engage in lecture-facilitated large group discussions
  - reflect on which submissions come top

Thank you

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(Moodle plug-in)

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